

Class XII

Chapter 6- Application of Derivatives

Topic – Tangents and Normals

Worksheet (Standard)

1. At point on the curve $y=x^2$ does the normal make an angle of 30° clockwise with the x-axis. (2)
2. Find the equation normal to the curve $x^{2/3} + y^{2/3} = 2$ at the point (1,1)(2)(HOTS)
3. Find the equation of tangent to the curve given by $x=asin^3t, y=bcos^3t$ at a point where $t= \pi/2$ (2)
4. Find the points on the curve $9y^2 = x^3$, where the normal to the curve makes equal intercepts with the axes. (2)
5. Find the points on the curve $x^2/4 + y^2/25=1$ at which the tangents are parallel to the X-axis. (2)
6. Find the point on the curve $y=3x^2 + 4$ at which the tangent is perpendicular to the line with slope $(-1/6)$ (2)
7. Find the points on the curve $x^2/16 + y^2/81=1$ at which the tangents are parallel to the Y-axis. (2)
8. If the curves $y=2ex$ & $y=ae^{-x}$ intersect orthogonally, What is the value of a ? (2)
9. Show that the normal at any point θ to the curve $x= a\cos\theta + a\sin\theta, y=asin\theta - a\theta\cos\theta$ is at constant distance from the origin.(4)
10. Prove that the line $x/a + y/b = 1$ is a tangent to the curve $y=be^{-x/a}$ at the point where the curve cuts Y-axis.(4)
11. The curve $y=ax^3+bx^2+cx+5$ touches the x-axis at the point $(-2,0)$ and Cuts the y-axis at a point where the slope is 3. Find a, b, c (4)
12. Show that the curves $x= y^2$ & $xy=k$ cut at right angles if $8k^2= 1$ (4)
13. For the curve $y = 4x^3 - 2x^5$, find all the points at which the tangent passes through the origin.(4)
14. prove that the curves $y^2 = 4x$ & $x^2 + y - 6x + 1 = 0$ touch each other at the point (1,2)(4)
15. Find the co-ordinates of the point on the curve $x^{1/2} + y^{1/2} = 4$ at which tangent is equally inclined to the axes. (4)
16. Show that the curves $xy= a^2$ and $x^2 + y^2= 2a^2$ touch each other(4)
17. Find the equation of tangent to the curve $y=\cos(x+y)$, where $-2\pi < x < 2\pi$ (HOTS) (4)

18. Find the condition for the curves $x^2/a^2 - y^2/b^2 = 1, xy = c^2$ to intersect orthogonally. (4)

19.