## SUBJECT-MATHEMATICS, CLASS-XI CHAPTER-8 (BINOMIAL THEOREM) WORSHEET(BASIC)

Choose the correct option: (1 mark each)

- The coefficient of x<sup>5</sup> in the expansion of (x+3)<sup>8</sup> is (a)1022 (b) 1512 (c) 1215 (d) 2210
- The number of term in the expansion of (a-2b)<sup>22</sup> is
   (a) 21
   (b) 24
   (c) 23
   (d) 20

Fill in the blanks: (1 mark each)

- 3. The 9<sup>th</sup> term in the expansion of  $\left(\frac{x}{a} \frac{3a}{x^2}\right)^{12}$  is .....
- 4. If the fourth term in the expansion of  $\left(ax + \frac{1}{x}\right)^n$  is  $\frac{5}{2}$ , then the value of n is .....

## Answer the following: (1 mark each)

- 5. Write the general term in the expansion of  $(3x 2y)^{12}$
- 6. Find the middle term in the expansion of  $\left(3 \frac{x^3}{6}\right)^8$

## Short Answer Type Question (2 marks each)

- 7. Find the middle terms in the expansion of  $\left(2x^2 \frac{1}{x}\right)^7$
- 8. Find the term independent of x in the expansion of  $\left(\frac{3}{2}x^2 \frac{1}{3x}\right)^6$

## Long answer type question-I : (4 marks each)

9.Using binomial theorem prove that  $9^{n+1} - 8n - 9$  is divisible by 64, whenever n is a positive integer.

10.Show that the middle term in the expansion of  $(1 + x)^{2n}$  is  $\frac{1 \cdot 3 \cdot 5 \dots (2n-1)}{n!} 2n x^{n}$ 

## Long answer type question-II : (6 marks each)

- 11. The second ,third and fourth terms in the binomial expansion (x+a)<sup>n</sup> are 240,720 and 1080, respectively. Find x ,a and n.
- 12. The coefficients of the  $(r-1)^{th}$ ,  $r^{th}$  and  $(r+1)^{th}$  terms in the expansion  $(x+1)^{n}$  are in the ratio

1:3:5.Find n and r.

### DAV PUBLIC SCHOOL, KALINGANAGAR, BHUBANESWAR

## SUBJECT-MATHEMATICS, CLASS-XI CHAPTER-8 (BINOMIAL THEOREM) WORSHEET(STANDARD)

**Choose the correct option: (1 mark each)** 

1. If the coefficient of x<sup>7</sup> and x<sup>8</sup> in the expansion of  $\left(2 + \frac{x}{3}\right)^n$  are equal, then n is

(a)56 (b) 55 (c) 45 (d) 15

2. The total number of term in the expansion of (x+a)<sup>100</sup>+ (x-a)<sup>100</sup> after simplification is
(a) 50 (b) 202 (c) 51 (d) none of these

Fill in the blanks: (1 mark each)

3. The 4<sup>th</sup> term from end in the expansion of  $\left(\frac{x^3}{2} - \frac{2}{x^2}\right)^9$  is .....

4. Middle term in the expansion of  $(a^3 + ba)^{28}$  is ..... Answer the following: (1 mark each)

5. Find the r<sup>th</sup> term in the expansion of  $\left(x + \frac{1}{x}\right)^{2r}$ .

6. Find the coefficient of  $x^{11}$  in the expansion of  $\left(x^3 - \frac{2}{x^2}\right)^{12}$ 

### Short Answer Type Question (2 marks each)

7. Find the middle term( terms ) in the expansion of  $\left(\frac{p}{x} + \frac{x}{p}\right)^9$ 

8.If the coefficients of  $(r-5)^{th}$  and  $(2r-1)^{th}$  terms of the expansion of  $(1+x)^{34}$  are equal ,find r Long answer type question-I : (4 marks each)

9. Find the coefficient of  $a^4$  in the product  $(1 + 2a)^4(2 - a)^5$  using binomial theorem.

10. If in the expansion of  $(1 + x)^n$ , the coefficients of  $14^{th}$ ,  $15^{th}$  and  $16^{th}$  terms are in A.P., find n.

### Long answer type question-II : (6 marks each)

11. If the coefficients of  $a^{r-1}$ ,  $a^r$  and  $a^{r+1}$  in the expansion of  $(1 + a)^n$  are in arithmetic progression, prove that  $n^2 - n(4r + 1) + 4r^2 - 2 = 0$ .

12. If three consecutive coefficients in the expansion of  $(1 + x)^n$  are in the ratio 6:33:110,

find n and r.

### DAV PUBLIC SCHOOL, KALINGANAGAR, BHUBANESWAR

## SUBJECT-MATHEMATICS, CLASS-XI CHAPTER-8 (BINOMIAL THEOREM) WORSHEET(ADVANCE)

#### **Choose the correct option: (1 mark each)**

- 1. The coefficient of  $x^p$  and  $x^q$  (p and q are positive integers) in the expansion of  $(1 + x)^{p+q}$  are
  - (a) Equal (b) equal with opposite signs (c)reciprocal of each other (d)none of these
- 2. The ratio of the coefficient of  $x^{15}$  to the term independent of x in  $\left(x^2 + \frac{2}{x}\right)^{15}$  is

(a) 12:32 (b) 1:32 (c) 32:12 (d) 32:1

- Fill in the blanks: (1 mark each)
  - 3. The number of terms in the expansion of  $(x + y + z)^n$  is .....
  - 4. In the expansion of  $\left(x^2 \frac{1}{x^2}\right)^{16}$ , the value of constant term is .....

#### Answer the following: (1 mark each)

- 5. Determine whether the expansion of  $\left(x^2 \frac{2}{x}\right)^{18}$  will contain a term containing  $x^{10}$ ?
- 6. Find the middle term in the expansion of  $\left(2ax \frac{b}{x^2}\right)^{12}$

#### Short Answer Type Question (2 marks each)

- 7. If n is a positive integer, find the coefficient of  $x^{-1}$  in the expansion of  $(1+x)^n \left(1+\frac{1}{x}\right)^n$
- 8. If p is a real number and if the middle term in the expansion of  $\left(\frac{p}{2}+2\right)^8$  is 1120, find p.

## Long answer type question-I : (4 marks each)

- 9. Find n ,if the ratio of the fifth term from the beginning to the fifth term from end in the expansion of  $\left(\sqrt[4]{2} + \frac{1}{\sqrt[4]{3}}\right)^n$  is  $\sqrt{6}$ : 1
- 10. Using binomial theorem, show that  $3^{4n+1} + 16n 3$  is divisible by 256 if n is a positive integer.
- 11. If the coefficient of second ,third and fourth terms in the expansion of  $(1 + x)^{2n}$  are in A.P. Show that  $2n^2 9n + 7 = 0$
- 12. In the expansion of  $(x + a)^n$  if the sum of odd terms is denoted by O and the sum of even term by E. Then prove that

(i)
$$O^2 - E^2 = (x^2 - a^2)^n$$
  
(ii) $4OE = (x + a)^{2n} - (x - a)^{2n}$ 

# Long answer type question-II : (6 marks each)

- 13. Find the term independent of x in the expansion of  $(1 + x + 2x^3) \left(\frac{3}{2}x^2 \frac{1}{3x}\right)^9$ .
- 14. If  $a_1$ ,  $a_2$ ,  $a_3$  and  $a_4$  be any four consecutive coefficients in the expansion of  $(1 + x)^n$ , Prove that  $\frac{a_1}{a_1 + a_2} + \frac{a_3}{a_3 + a_4} = \frac{2a_2}{a_2 + a_3}$