

SUBJECT – MATHEMATICS , CLASS-XII(HOTS)
CHAPTER-INCREASING & DECREASING

- 1- Show that the function $f(x)=2x+\cot^{-1}x+\log(\sqrt{1+x^2}-x)$ is increasing on \mathbb{R}
- 2- Prove that the function $f(x)=\tan x-4x$ is strictly decreasing on $(-\frac{\pi}{3}, \frac{\pi}{3})$
- 3- Prove that $f(x)=\frac{4\sin x}{2+\cos x}-x$ is an increasing function of x in $(0, \frac{\pi}{2})$
- 4- Find the interval in which $f(x)=\frac{x}{\log x}$ is increasing or decreasing
- 5- Find the interval $f(x)=\begin{vmatrix} x+a^2 & ab & ac \\ ab & x+b^2 & bc \\ ac & bc & x+c^2 \end{vmatrix}$ is increasing or decreasing where a, b, c are any real number.
- 6- Prove that $\sin(\tan x) > x$, for all $x \in (0, \frac{\pi}{2})$
- 7- If $f(x)=x^3+bx^2+cx+d$ prove that $f(x)$ is increasing for all real x if $0 < b^2 < c$
- 8- Show that $2\sin x + 2\tan x \geq 3x$, where $0 \leq x \leq \frac{\pi}{2}$.
- 9- Show that $1+x\log(x+\sqrt{1+x^2}) \geq \sqrt{1+x^2}$, for all $x \geq 0$
- 10- Given that $A=\{x: \frac{\pi}{6} \leq x \leq \frac{\pi}{3}\}$ and $f(x)=\cos x-x(1+x)$, find $f(A)$