

# DAV PUBLIC SCHOOL, IFFCO, PARADEEP

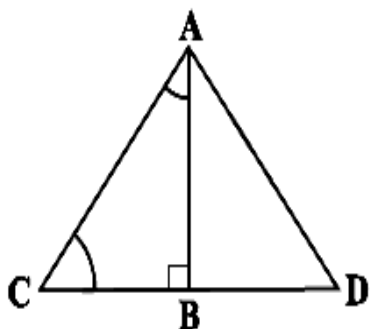
CLASS-IX

SUB-MATHEMATICS

TOPIC-TRIANGLES

WORKSHEET-HOTS

1. ABC is a triangle with  $\angle B = 2\angle C$ . D is a point on BC such that AD bisects  $\angle BAC$  and  $AD=CD$ . Prove that  $\angle BAC = 72^\circ$ .
2. Bisectors of the angles B and C of an isosceles triangle with  $AB = AC$  intersect each other at O. BO is produced to a point M. Prove that  $\angle MOC = \angle ABC$ .
3. ABC is a right triangle and right angled at B such that  $\angle BCA = 2 \angle BAC$ . Show that hypotenuse  $AC = 2 BC$ .



4. If the bisector of an angle of a triangle also bisects the opposite side, prove that the triangle is isosceles.
5. O is a point in the interior of a square ABCD such that OAB is an equilateral triangle. Show that  $\triangle OCD$  is an isosceles triangle.
6. Show that in a quadrilateral ABCD,  $AB + BC + CD + DA < 2(BD + AC)$
7. In a triangle ABC, D is the mid-point of side AC such that  $BD = \frac{1}{2} AC$ . Show that  $\angle ABC$  is a right angle.
8. In a right triangle, prove that the line-segment joining the mid-point of the hypotenuse to the opposite vertex is half the hypotenuse.

9. ABC is a right triangle such that  $AB = AC$  and bisector of angle C intersects the side AB at D. Prove that  $AC + AD = BC$ .
10. AB and CD are the smallest and largest sides of a quadrilateral ABCD. Out of  $\angle B$  and  $\angle D$  decide which is greater.
11. ABCD is quadrilateral such that  $AB = AD$  and  $CB = CD$ . Prove that AC is the perpendicular bisector of BD.
12. Line segment joining the mid-points M and N of parallel sides AB and DC, respectively of a trapezium ABCD is perpendicular to both the sides AB and DC. Prove that  $AD = BC$ .